

Trabecular shear stress amplification and variability in human vertebral cancellous bone: Relationship with age, gender, spine level and trabecular architecture

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Abstract

Trabecular shear stress magnitude and variability have been implicated in damage formation and reduced bone strength associated with bone loss for human vertebral bone. This study addresses the issue of whether these parameters change with age, gender or anatomical location, and if so whether this is independent of bone mass. Additionally, 3D-stereology-based architectural parameters were examined in order to establish the relationship between stress distribution parameters and trabecular architecture. Eighty cancellous bone specimens were cored from the anterior region of thoracic T12 and donor-matched lumbar L1 vertebrae from a randomly selected population of 40 cadavers. The specimens were scanned at 21- μ m voxel size using microcomputed tomography (μ CT) and reconstructed at 50 μ m. Bone volume fraction (BV/TV), trabecular number (Tb.N), trabecular thickness (Tb.Th), trabecular separation (Tb.Sp), bone surface-to-volume ratio (BS/BV), degree of anisotropy (MIL1/MIL3), and connectivity density ($-\#Euler/Vol$) were calculated directly from micro-CT images. Large-scale finite element models were constructed and superior-inferior compressive loading was simulated. Apparent cancellous modulus (E_{FEM}) was calculated. The average trabecular von Mises stress generated per uniaxial apparent stress ($\bar{\sigma}_{VM}/\sigma_{app}$) and coefficient of variation of trabecular von Mises stresses (COV) were calculated as measures of the magnitude and variability of shear stresses in the trabeculae. Mixed-models and regression were used for analysis. $\bar{\sigma}_{VM}/\sigma_{app}$ and COV were not different between genders and vertebrae. Both $\bar{\sigma}_{VM}/\sigma_{app}$ and COV increased with age accompanied by a decrease in BV/TV. Strong relationship of $\bar{\sigma}_{VM}/\sigma_{app}$ with BV/TV was found whereas COV was strongly related to $E_{FEM}/(BV/TV)$. The results from T12 and L1 were not different and highly correlated with each other. The relationship of $\bar{\sigma}_{VM}/\sigma_{app}$ with COV was observed to be different between males and females. This difference could not be explained by architectural parameters considered in this study. Our results support the relevance of trabecular shear stress amplification and variability in age-related vertebral bone fragility. The relationships found are expected to help understand the micro-mechanisms by which cancellous bone mass and mechanical properties are modulated through a collection of local stress parameters.

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Introduction

Increase of trabecular stress variability with loss of bone mass has been implicated as a mechanism for increased cancellous bone fragility with age and disease [11,35]. The underlying notion was that increased variability in trabecular stresses would give rise to stress concentrations resulting in a reduction of bone strength. Consistent with this notion, coefficient of variation of trabecular von Mises stress distributions (COV) as estimated

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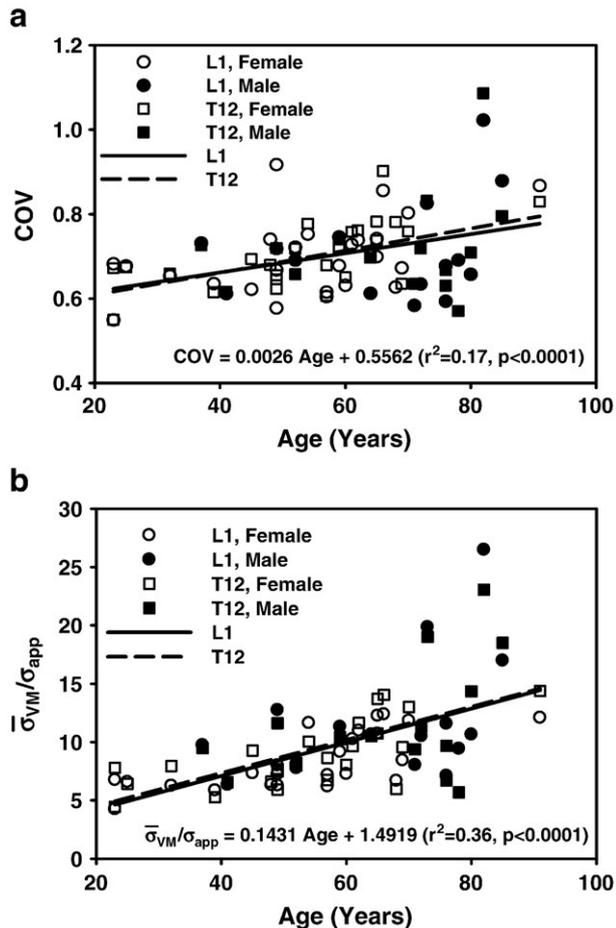


Fig. 1. Both COV and $\bar{\sigma}_{VM}/\sigma_{app}$ increased with age in T12 and L1 ($0.14 < r^2 < 0.37$, $p < 0.0001$ to $p < 0.02$). These increases with age were not different between T12 and L1 ($p > 0.58$) or between males and females ($0.47 < p < 0.88$). Regressions are for pooled data.

from microcomputed tomography (μ CT)-based finite element (FE) calculations has been shown to increase with decreasing bone volume (BV/TV) accompanied by a decrease in strength in human vertebral cancellous bone. It has also been shown that there is a significant positive correlation between COV and the density of in vivo microdamage from the same region in human vertebrae [34].

Average trabecular von Mises stress per apparent uniaxial stress ($\bar{\sigma}_{VM}/\sigma_{app}$) as estimated from finite element (FE) calculations was proposed as a structural index that represents the tendency of the cancellous structure to amplify shear stresses in the tissue [35]. This parameter, too, has been shown to correlate with the density of in vivo microdamage in human vertebral bone [34]. It should be noted that, though only moderately explanatory, COV and $\bar{\sigma}_{VM}/\sigma_{app}$ had the strongest correlations ever demonstrated with in vivo microdamage in cancellous bone among mechanical parameters considered thus far. In addition, it was observed that the tissue from the thoracic 12-lumbar 1 junction had the largest $\bar{\sigma}_{VM}/\sigma_{app}$ [35] accompanied by the lowest strength [36] suggesting that this parameter may be relevant to the high incidence of vertebral fractures at these spine levels [2,3,10,12,16,20,23,26].

Together, trabecular shear stress distribution parameters, namely COV and $\bar{\sigma}_{VM}/\sigma_{app}$, appear important in understanding the mechanistic consequence of bone loss and trabecular adaptation. However, it is not known whether these parameters change with age and if so, whether these changes are independent of changes in bone volume or gender and type of vertebral bone. Secondly, which microstructural parameters of cancellous bone can explain stress distribution parameters is unknown. Also not known is whether shear stress parameters in tissue from one vertebra can be predicted by those in tissue from another vertebra of the same individual. Our objective was to answer these questions for thoracic 12 (T12) and lumbar 1 (L1) vertebrae from the same individuals.

Methods

Thoracic 12 and L1 vertebrae were collected fresh from 15 male (66 ± 15 yrs) and 25 female (54 ± 16 yrs) cadavers. Because complete medical history was not available for all donors, all cadavers were included without screening for bone diseases. Eight-mm-diameter and 10-mm-long cylindrical cancellous bone specimens were prepared from the anterior region of vertebral bodies in the superoinferior direction as described previously [15,30]. Only one specimen from each vertebra was prepared and all donors had both their T12 and L1 represented in the sample population.

The specimens were scanned using an in-house microcomputed tomography system [24] at a voxel size of $21 \mu\text{m}$. Large-scale, linear finite element models with uniform isotropic element properties (Young's modulus = 5 GPa, Poisson's ratio = 0.3) were constructed and solved using an element size of $50 \mu\text{m}$ and fixed boundary conditions as described previously [15,31]. Displacements corresponding

Table 1
The mean (standard deviation) of measured parameters from thoracic 12 and lumbar 1 vertebrae

Parameter	Thoracic 12	Lumbar 1	Difference%	Difference (p)	Correlation (r)
-#Euler/Vol (mm^{-3})	0.3884 (0.1662)	0.3673 (0.1498)	5.4	0.047	0.92
BV/TV	0.1445 (0.0447)	0.1477 (0.0439)	-2.2	0.277	0.92
BS/BV (mm^{-1})	8.867 (0.906)	8.645 (0.791)	2.5	0.013	0.81
Tb.Th (mm)	0.2280 (0.0242)	0.2333 (0.0217)	-2.3	0.028	0.80
Tb.N (mm^{-1})	0.6276 (0.1539)	0.6272 (0.1509)	0.1	0.963	0.93
Tb.Sp (mm)	1.473 (0.486)	1.470 (0.494)	0.2	0.899	0.95
MIL1/MIL3	1.641 (0.163)	1.642 (0.191)	0.0	0.976	0.73
E_{FEM} (MPa)	260 (116)	268 (117)	-3.3	0.398	0.85
COV	0.7090 (0.0962)	0.7034 (0.1014)	0.8	0.593	0.77
$\bar{\sigma}_{VM}/\sigma_{app}$	9.942 (3.943)	9.736 (4.118)	2.1	0.375	0.94

Percent difference in means, significance of these differences (as determined from paired t -tests) and correlations between vertebrae are indicated. An adjustment for multiple tests, taking into account the correlations between all parameters, suggested a p -value of 0.018 to be considered as significant for an α of 0.05.

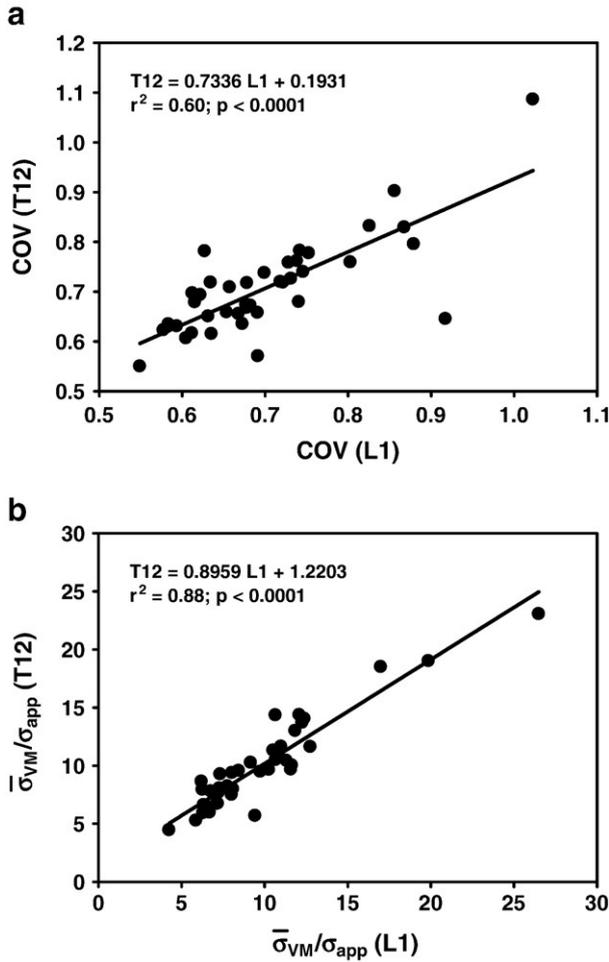


Fig. 2. COV and $\bar{\sigma}_{VM}/\sigma_{app}$ from T12 are highly correlated with those from L1 in the same individual.

to a strain of 0.005 were applied to the models in the superoinferior direction. A six-node Beowulf cluster with 8GB of main memory was used for solving the FE models.

The mean ($\bar{\sigma}_{VM}$) and standard deviation ($\hat{\sigma}_{VM}$) of trabecular von Mises stress distribution were calculated from a 3-parameter Weibull cumulative probability function fitted to the stress distribution for each specimen [11,31,34,35]. The variability of trabecular shear stress was expressed as the coefficient of variation:

$COV = \hat{\sigma}_{VM}/\bar{\sigma}_{VM}$. The magnitude of trabecular shear stress was expressed as the average trabecular shear stress per apparent superoinferior uniaxial stress, σ_{app} , where $\bar{\sigma}_{VM}/\sigma_{app}$ is considered a structural index of shear stress amplification in the hard tissue. The apparent uniaxial stress was calculated by summing nodal reaction forces and dividing by the apparent cross-sectional area of specimens. Apparent modulus (E_{FEM}) was calculated from the displacement input and reaction forces at the boundary nodes.

Bone volume fraction (BV/TV), trabecular number (Tb.N), trabecular thickness (Tb.Th), trabecular separation (Tb.Sp), bone surface-to-volume ratio (BS/BV), degree of anisotropy (ratio of mean intercept lengths in principal directions; MIL1/MIL3), and connectivity density (-#Euler/Vol) were calculated directly from micro-CT images using 3D-stereological procedures as described previously [9,13,19].

PROC MIXED procedures of SAS (Cary, NC) were used to examine the effect of vertebra type, gender, BV/TV and age on COV and $\bar{\sigma}_{VM}/\sigma_{app}$, with vertebra type introduced as a repeated factor with two levels (T12 and L1). Relationships were assessed using regression analysis. Statistical significance was set as $p < 0.05$. p -values corresponding to an α of 0.05 were indicated for multiple tests, taking into account the correlations between parameters [25].

Results

COV and $\bar{\sigma}_{VM}/\sigma_{app}$ were not different between T12 and L1 ($p > 0.76$ and $p > 0.07$, respectively) or between males and females ($p > 0.54$ and $p > 0.18$, respectively) after accounting for age. Age was significantly associated with both COV ($p < 0.0044$) and $\bar{\sigma}_{VM}/\sigma_{app}$ ($p < 0.0004$) (Fig. 1), however, there was no longer any association between age and the outcomes ($p > 0.33$) with adjustment for BV/TV.

COV, $\bar{\sigma}_{VM}/\sigma_{app}$ and microstructural parameters from T12 were significantly correlated to those from L1 in an individual (Table 1, Fig. 2). Significant but small differences in -#Euler/Vol, BS/BV and Tb.Th were found between T12 and L1 (Table 1).

The relationships of mechanical with microstructural parameters were not different between T12 and L1 (p -values between 0.593 and 0.998; ANCOVA). Data were pooled over T12 and L1 for further analyses of relationships between mechanical and microstructural parameters. Significant correlations of COV and $\bar{\sigma}_{VM}/\sigma_{app}$ with BV/TV and other microstructural parameters were found (Table 2). Multiple regressions indicated that anisotropy and BV/TV independently contributed to COV and $\bar{\sigma}_{VM}/\sigma_{app}$ (Table 3).

Correlations of COV and $\bar{\sigma}_{VM}/\sigma_{app}$ with single variables that were higher than those with multiple variables were found when

Table 2
Matrix of Pearson’s correlation coefficients (r)

	Age	-#Euler/Vol	BV/TV	BS/BV	Tb.Th	Tb.N	Tb.Sp	MIL1/MIL3	E_{FEM}	COV	$\bar{\sigma}_{VM}/\sigma_{app}$
Age	1	-0.52	-0.64	0.38	-0.39	-0.63	0.60	0.27	-0.62	0.42	0.60
-#Euler/Vol		1	0.68	0.03	0.00	0.84	-0.77	-0.14	0.56	-0.40	-0.60
BV/TV			1	-0.66	0.68	0.94	-0.88	-0.18	0.95	-0.64	-0.85
BS/BV				1	-0.99	-0.39	0.36	0.15	-0.70	0.43	0.54
Tb.Th					1	0.41	-0.38	-0.15	0.72	-0.43	-0.54
Tb.N						1	-0.95	-0.14	0.87	-0.63	-0.85
Tb.Sp							1	0.10	-0.81	0.66	0.92
MIL1/MIL3								1	-0.05	-0.36	-0.02
E_{FEM}									1	-0.78	-0.86
COV										1	0.80
$\bar{\sigma}_{VM}/\sigma_{app}$											1

An adjustment for multiple tests, taking into account the correlations between parameters, suggested a p -value of 0.005 to be considered as significant for an α of 0.05.

$|r| \geq 0.36$; $p < 0.001$.

$|r| \geq 0.26$; $p < 0.05$.

Table 3
Multiple regression models for COV and $\bar{\sigma}_{VM}/\sigma_{app}$

Term	Estimate	t ratio	p<
<i>COV</i> ($r^2_{adj}=0.64$; $p<0.001$)			
Intercept	1.400	19.8	0.001
BV/TV	-1.629	-10.68	0.001
MIL1/MIL3	-0.278	-7.3	0.001
$\bar{\sigma}_{VM}/\sigma_{app}$ ($r^2_{adj}=0.77$; $p<0.001$)			
Intercept	29.70	12.6	0.001
BV/TV	-48.32	-3.2	0.002
Tb.N	-9.96	-2.3	0.001
MIL1/MIL3	-3.99	-3.2	0.002

Models were constructed using a stepwise regression that included BV/TV, Tb. N, #Euler/Vol and MIL1/MIL3 as explanatory variables. BV/TV was forced to stay in the model in order to determine contributions from other variables that are independent of BV/TV.

nonlinear relationships were considered. A strong negative linear relationship was found between COV and finite element calculated apparent modulus normalized with bone volume fraction ($E_{FEM}/(BV/TV)$) ($r^2=0.87$; $p<0.0001$, Fig. 3a). The

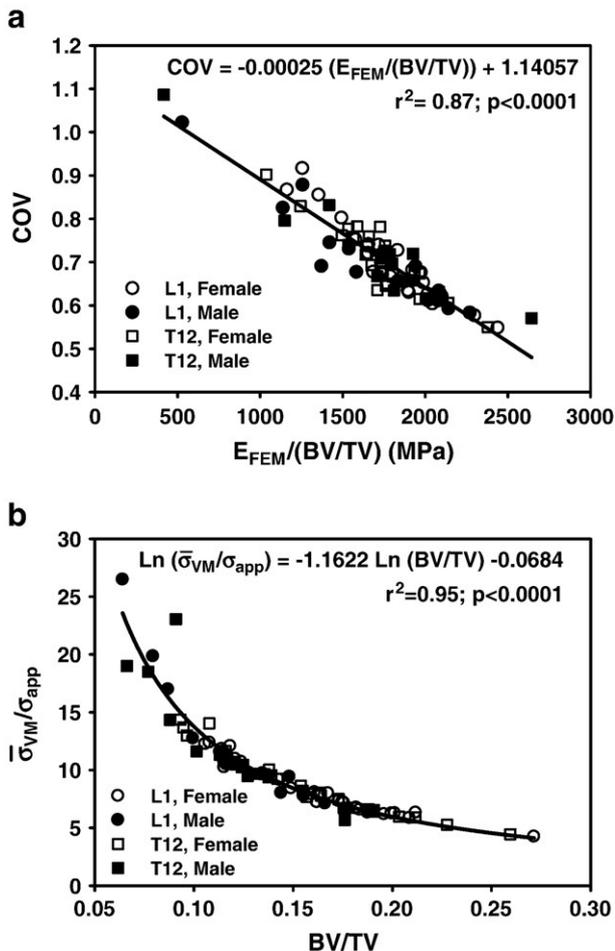


Fig. 3. (a) COV decreased linearly with increasing $E_{FEM}/(BV/TV)$. (b) Negative log–log relationship between $\bar{\sigma}_{VM}/\sigma_{app}$ BV/TV showing that $\bar{\sigma}_{VM}/\sigma_{app}$ decreased nonlinearly with increasing BV/TV.

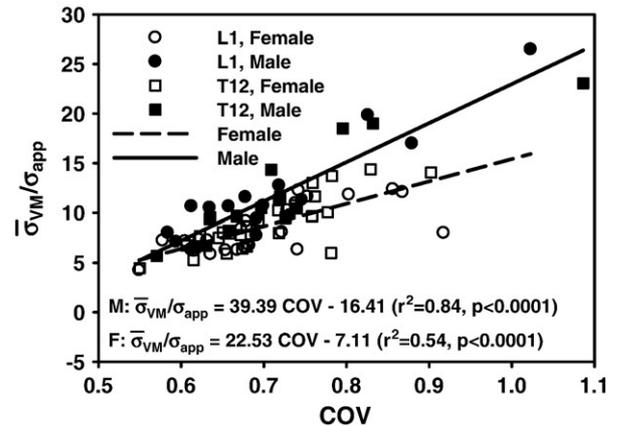


Fig. 4. COV and $\bar{\sigma}_{VM}/\sigma_{app}$ are more strongly related in males than in females. The slopes of regressions are statistically different, even after accounting for age ($p<0.0001$).

strongest relationship of $\bar{\sigma}_{VM}/\sigma_{app}$ was with BV/TV raised to the power -1.1622 ($r^2=0.96$; $p<0.0001$, Fig. 3b).

Although COV and $\bar{\sigma}_{VM}/\sigma_{app}$ were positively related ($r^2=0.64$, $p<0.0001$), the relationship was different between males and females ($p<0.0001$ in age-adjusted models) (Fig. 4). This gender dependence could not be explained by any combination of stereological parameters considered here (the interaction between gender and COV remained significant at $p<0.0001$ in all models of $\bar{\sigma}_{VM}/\sigma_{app}$).

Discussion

We demonstrated that the magnitude of trabecular shear stresses relative to the compressive stress applied on the tissue ($\bar{\sigma}_{VM}/\sigma_{app}$) and their nonuniformity (COV) increase with age. These increases were explainable by the negative relationship between bone mass and age. However, this does not mean that the stress parameters are not important once bone mass is taken into account but rather points to a mechanistic consequence of bone loss with aging. These findings are consistent with the idea that a direct consequence of structural changes due to bone loss associated with aging is increased localized stresses at the hard tissue level. Although our analyses are elastic and failure is not explicitly simulated, the decrease in the mean and COV of the shear stress with bone mass suggest that cancellous bone structure is adapted to control stress concentration.

Increasing tissue apparent modulus per available bone mass has been proposed as an optimizing strategy for cancellous structure [29]. Since the amount of material under extreme values of stresses would be reduced in a stiffness-optimized structure, our finding that COV of shear stresses are tightly related to $E_{FEM}/(BV/TV)$ is consistent with this proposal. Thus controlling shear stress variability would provide a mechanism, active at the hard tissue level, for optimization of modulus for a given bone mass. While a composite variable such as $E_{FEM}/(BV/TV)$ was most explanatory for COV, much of the variability in mean von Mises stress amplification ($\bar{\sigma}_{VM}/\sigma_{app}$) could be explained by BV/TV alone, also consistent with the notion that tissue level stresses are being controlled on the average (*i.e.*, the microstructure is designed to

control average properties). The strong correlation of COV with $E_{FEM}/(BV/TV)$ and that of $\bar{\sigma}_{VM}/\sigma_{app}$ with BV/TV indicate that the average and the variability of trabecular stresses are related but they are not entirely equivalent. It should be noted that the relationships (between COV and $E_{FEM}/(BV/TV)$, and between $\bar{\sigma}_{VM}/\sigma_{app}$ and BV/TV) found in this study provided much higher r^2 values than those existing between COV and BV/TV alone [11,34,35]. The relationships reported in this study may provide a more refined guide than those in previous reports for further research into how the regulation of apparent level (average) properties can be achieved by sensing and responding to the local (cellular level) mechanical environment.

Current results indicate that the dependence of $\bar{\sigma}_{VM}/\sigma_{app}$ on COV of trabecular von Mises stress is statistically different between males and females. This difference suggests that the response of bone to changes in mechanical loading could be different between genders. It is possible that the difference is explained by sexual dimorphism in vertebral cancellous bone osteocyte density [28]. Vertebral osteocyte density is greater in women than in men [28], suggesting that the density of mechanosensory cells and potentially the ability to respond to loading are gender-specific. We suggest that the difference in the correlation of $\bar{\sigma}_{VM}/\sigma_{app}$ and COV between males and females is caused by the differences in anatomy [28] and pattern of bone loss [22] between genders. The dimorphism in the coupling of these parameters and their potential association with dimorphism in the osteocyte network may be a key to understanding the gender-specific differences in the modulation of cancellous bone structure [1,33].

Note that although both $\bar{\sigma}_{VM}/\sigma_{app}$ and COV are correlated to BV/TV and trabecular architecture, the architectural parameters examined here cannot explain the gender dependence of the relationship between the two stress parameters. Also note that, by using homogenous element moduli, we have isolated the effect of structural properties from that of hard tissue material properties. Therefore, the obtained results cannot be attributed to modulus variability within the cancellous bone. The architectural parameters examined in this study are based on stereological principles. Stereology-based calculation of microstructural parameters results in values that are different from those obtained by direct calculation [7,14] but microstructural parameters calculated using one method are highly correlated to those calculated using the other method [7]. Perhaps more importantly, the microstructural parameters measured in this study represent an average geometry, density or ratio for a given cancellous structure. The results indicate that structural parameters other than those considered in the current study, including parameters that can represent the variability of the microstructure, would be necessary to understand the relationship between stress amplification and variability.

No difference was found in the measured parameters and their relationship with bone mass, age or gender between L1 and T12 levels. In fact, shear stress magnitude and variability in one vertebra was predictable from those in the adjacent vertebra for a given individual. This is consistent with our initial observation that the stress distribution properties of the cancellous tissue from vertebrae at these adjacent locations are similar [35]. The

similarity of results from two adjacent but anatomically distinct vertebrae suggests that the stress distribution parameters are related to systemic factors or those that can affect the T12–L1 segment of the spine. It remains to be demonstrated whether the association of stress parameters between vertebrae is maintained for vertebrae that are far apart.

Some limitations should be noted. The FE models were constructed from images coarsened to 50- μm voxel size and utilized homogeneous and isotropic material properties. Twenty-one μm is the best possible voxel size that can be achieved for specimens of the current size in our tomography system. We have previously demonstrated that parameters calculated from images scanned at 21 μm and reconstructed at 50 μm were not significantly different and correlated with an r^2 value of 0.91 or higher [31] (the relationships presented in Figs. 3a and b were confirmed using an independent set of human vertebral cancellous bone specimens ($n=31$, $BV/TV=0.13\pm 0.04$, $Tb.Th=0.108\pm 0.016$ mm) scanned and processed at 27- μm voxel size). The apparent modulus calculated from FE models is affected by the hard tissue (element) modulus distributions determined by CT-attenuation value distributions [4]. However, there is no established method of converting CT-attenuation values to hard tissue moduli and the variability of tissue moduli depends on the formulae used in the conversion. Our analyses suggest that the change in apparent modulus due to modulus variability only is small in human vertebral cancellous bone when up to a third order relationship is used to convert CT-attenuation values to element moduli [18]. Furthermore, the FE-calculated cancellous modulus from homogenous and isotropic models has been highly predictive of experimentally measured cancellous modulus in previous studies of human vertebral bone indicating that calculation of stresses using the current model is reasonably accurate [15,32]. The selection of the von Mises stress as a measure of a damaging form of stress and the calculation of the stress parameters were discussed at length in our previous publications [11,34,35]. These are the same conditions used in studies where our observations that motivated this study were made [11,34,35]. Together, these limitations are expected to have minor effects on our results but not affect our conclusions about cancellous tissue.

This study was also limited to an investigation of the cancellous tissue from the anterior region. Although one would ultimately wish to understand how the strength of a whole vertebra can be affected by stress distribution parameters, the importance of the quality of cancellous tissue in mechanical health of the whole vertebra cannot be denied. Many of the investigations on the contribution of cancellous and cortical tissue to the strength of vertebra used finite element models. These models, all having different levels of structural accuracy, estimated a varying degree of importance (10%–63%) for the cortical shell relative to the cancellous centrum [5,8,27]. However, experimental studies reported only a 10% contribution of cortical shell to vertebral strength [21]. Furthermore, the bone density measured in similar regions to ours has been shown to strongly correlate to fracture load for the T12–L1 levels [6]. In our own experience, cancellous bone properties from regions similar to those examined in the current study were highly correlated with the strength of a whole vertebral body [17],

consistent with the findings of Cody et al. [6]. It is clear that cancellous tissue from the analyzed regions is relevant to whole vertebral strength. As such, this study addresses several questions related to vertebral bone tissue quality and is not focused on predicting vertebral strength.

In summary, we have determined the relationships between trabecular shear stress parameters, apparent mechanical properties, bone architecture, gender and age for human vertebral cancellous bone. The demonstration of these relationships is a step towards better defining the micro-mechanisms by which bone mass and mechanical properties interact and lead to age-related bone fragility.

Acknowledgments

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